

WARGAMING ULTRA-FAST PROPAGATION ALGORITHMS FOR FASTPROP

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1. OVERVIEW

The purpose of this paper is to describe a set of algorithms that provide ultra-fast simulation of propagation through the atmosphere. First, the requirement is established for this type of simulation as opposed to other valid types of simulation. Next, the reason for a new set of simulation algorithms is shown by pointing out the limitations of other methods. The main part of the paper describes the algorithms.

2. THE SIMULATION REQUIREMENT

The word "simulation" can apply to a variety of activities -- numerical solution of fluid flow, message traffic, pilot training in a flight simulator, and many more. An explicit meaning for "simulation" must be assigned or else there can be considerable confusion.

The purpose of a weather simulation in wargaming is to quantify the impact of weather on system performance. Once quantified, steps can be taken to optimize, procure, or reject the system. There are at least three categories of weather impact quantification:

2.1 System Physics and Engineering. The goal is to determine system limits, i.e. under what conditions will the system work.

2.2 System Effectiveness. How efficient is the system when deployed? This question is asked for a variety of situations from the simple one-on-one case up through theater level conflict. An important tenet sometimes overlooked is that extreme weather can defeat any system. The question is **WHERE** and **HOW OFTEN**? Another tenet often overlooked is that an offensive weapon can usually wait for good weather; the effectiveness of a defensive weapon is measured in all weather.

2.3 Training. Two different goals differentiate the role of weather in training.

2.3.1 In a Specified Syllabus, specific weather is needed that develops the desired skill.

The weather need not even be realistic - having five adjacent jet streams would quickly hone a pilots skill.

2.3.2 In a **Learning Exercise**, besides **learning** skills, lessons are **learned** about system usage, tactics, etc. Weather must be within the specified climate or else the wrong lessons will be learned.

The methods detailed in this paper are designed to meet goals 2.2 (system effectiveness) and 2.3.2 (learning exercises). However, these methods can be employed effectively for specified weather.

Of all weather impacts, **secability** (both passive and active -- **visual**, **IR**, radar) is needed at the most frequent intervals, requires the most calculations, and varies most rapidly. Although there is **more** to **secability** than just **transmission**, rapid calculation of propagation through the atmosphere is the vital first step. Propagation also **affects** radio and optical communications. Thus, the rest of this paper focuses on propagation.

Numerous calculations of propagation are generally required. The large number is due to the number of sensors and targets, and the fact that they can rapidly change location. For many applications, a complete scene must be rendered and displayed. In addition, many simulations require multiple views – as seen by a land observer, a pilot, a radar, an infrared sensor, etc. FASTPROP generates a virtual atmosphere scenario and then allows ultra-fast calculations within it.

3. THE DILEMMA

Facts and premises are only stated here. Justification is found in Boehm (1994c), Boehm (1995), Boehm (1996), and LaMar et al. (1994).

The atmosphere has layers that are effectively uniform with respect to transmission, but there are other layers, particularly those with clouds, that have intricate detail. It is the intricate detail that is hardest to specify and often has the strongest effect on propagation.

Current physical fluid dynamic methods cannot **specify** intricate details in the atmosphere. The basic problem is not the lack of computer power nor observations of initial or **boundary** conditions. It is due to lack of complete physical principles with respect to the stress **tensor**, water **droplet/crystal/vapor** transformation, and radiation flux in clouds. For example, the size of **cloud** puffs within a cloud can not be found using only first principle physics. That is not to say that such relationships will never be discovered, and work in such area should be encouraged. But the fact remains that there are unknown areas in the basic equations for turbulent motion and “in water transformations in the atmosphere.

Clouds and associated rain contribute the most to the variability of propagation, yet are poorly measured. Standard surface observations give **only** fractional cover and type -- no information is recorded on orientation, shape of gaps, or physical properties. Cloud types are based on visual appearance. The **liquid water** per cubic meter can vary over an order of magnitude within the same cloud type. Weather satellite data must use inferential methods of limited accuracy to determine cloud properties. Current archived observations fall **far** short of

specifying intricate detail in the atmosphere. Only a small fraction of atmospheric motion and constituents are actually measured.

Furthermore, **raw** observations contain a host of biases, idiosyncrasies, and instrument and archiving errors to fool the unwary simulator.

Current methods of calculating propagation are much too slow for operational simulation. MODTRAN running on a high end work station would take several days to calculate the radiances in a single picture.

A propagation beam is affected by structure of many scales -- **from** a single droplet on a sensor lens to a complete cloud **field** when viewed from hundreds of kilometers away as shown in Figure 1.

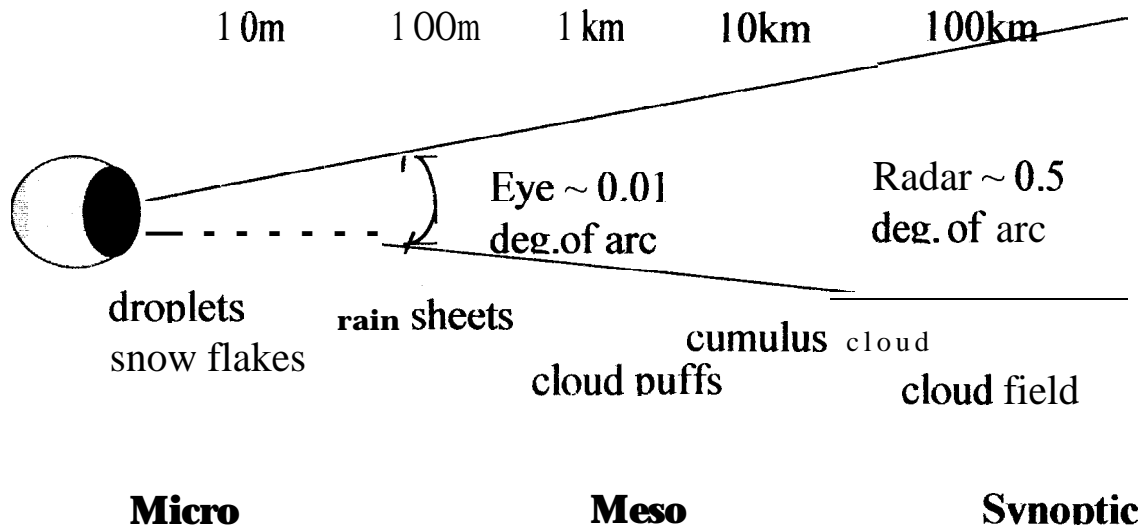


FIGURE 1. The scale of objects seen in a beam is a function of distance

Meteorologists have for many years divided atmospheric motion into various scales depending on what forces are important at that scale. Various scales, from a single droplet (e.g. on a lens) to large domains as seen by a distant millimeter system, are required for effective propagation simulations.

Propagation is along a beam which is not infinitesimally thin, but can often be described by a cone specified by some solid angle. The width of this cone at the target or at some atmospheric obstruction can be measured as the distance across the beam. There are beams which are very narrow (a centimeter or less in width), very short (less than 50 meters), very wide (10 km or more), or very long (500 km or more). What a sensor sees when looking through the atmosphere depends very much on its beam width and path length.

A meteorological satellite infrared sensor may have a beam width of 3 km or more at the height of the clouds. A high resolution surface based infrared sensor may have a beam width of

less than 5 meters when looking **at** the same cloud. What they see will not **have** the same **emissivity** nor structure. A realistic simulation must have the **ability to** provide propagation at various scales.

There **are** numerous statistical and **stochastic** models of the atmosphere **that** have been validated for specific purposes. These **range** from **simple rain/no rain Markov chains** to complex four-dimensional non-homogeneous **anisotropic** global models such as CFARC which produce minute **be** minute results for decades. **However**, a new kind of stochastic algorithm was needed to meet the ultra fast computation requirements.

4. Algorithm Design

In order to overcome the limitations of other methods, three methodologies were developed: 1. The **Morficon**, 2. Stochastic Indexing, and 3. HEFeS (Hierarchical Environmental Feature Structure). Together **the** three methods can form a weather expander. This weather **expander** takes a **small** set of input values and using stochastic generators produces a complete weather scenario.

4.1. The Morficon

Consider the calculation **of monochromatic** transmission **along** a beam,

$$I_s = I_T e^{\int_s^T K dx} \quad (1)$$

Where I_s is Illumination at sensor S

I_T is Illumination at target T

K is **the** absorption **coefficient**

x is along a line-of-sight

[f the line-of-sight is through a homogeneous layer, then the calculation is straight forward. **Many** transmission codes do just that; they assume a series of homogeneous layers.

In a region of intricate detail, a more general method is needed. A series of grid points **along** the line-of-sight **can** be defined and absorption interpolated to these points. However, a **regularly** spaced grid is inefficient. There are too many grid points where there is little change and too **few** where there is intricate detail.

The Morficon algorithm overcomes this shortcoming and **has** other desirable attributes as well. Instead of using ray tracing methods to render a scene, **radiometric** properties are precalculated for each object under various lighting conditions and stored as prototype objects called **morficons**. These **morficons** are stretched (morphed is the computer term) to adjust for viewing perspective, exact lighting, and individual shapes. By selecting a set of **morficons** based on physical and **climatological** principals, the resulting scene is consistent with the climatology

of the place and time and the physics of the atmosphere. For homogeneous or linear gradient objects, the transmission can rapidly be calculated using summations over objects,

$$I_s = I_t e^{-\sum_{i=1}^n K_i \Delta x_i} \quad \text{or} \quad \ln(I_s) = \ln(I_t) + \sum_{i=1}^n K_i \Delta x_i \quad (2)$$

where K_i is the absorption coefficient for the i th object or K_i is $(K_{\text{enter}} + K_{\text{exit}})/2$ for a linear gradient object. Subscripts enter and exit indicate where the line-of-sight enters and exits the 'object. Axis the distance along the line-of-sight through the object.

The morficon is not merely a computer trick to produce fast images, although it does appear to be one of the fastest ways to generate an image. Propagation calculations generally require various parameters to be integrated along a line of sight. Typically, a grid of these parameters is used to interpolate the parameters to spacing along the line of sight. These values are then summed to approximate the integration.

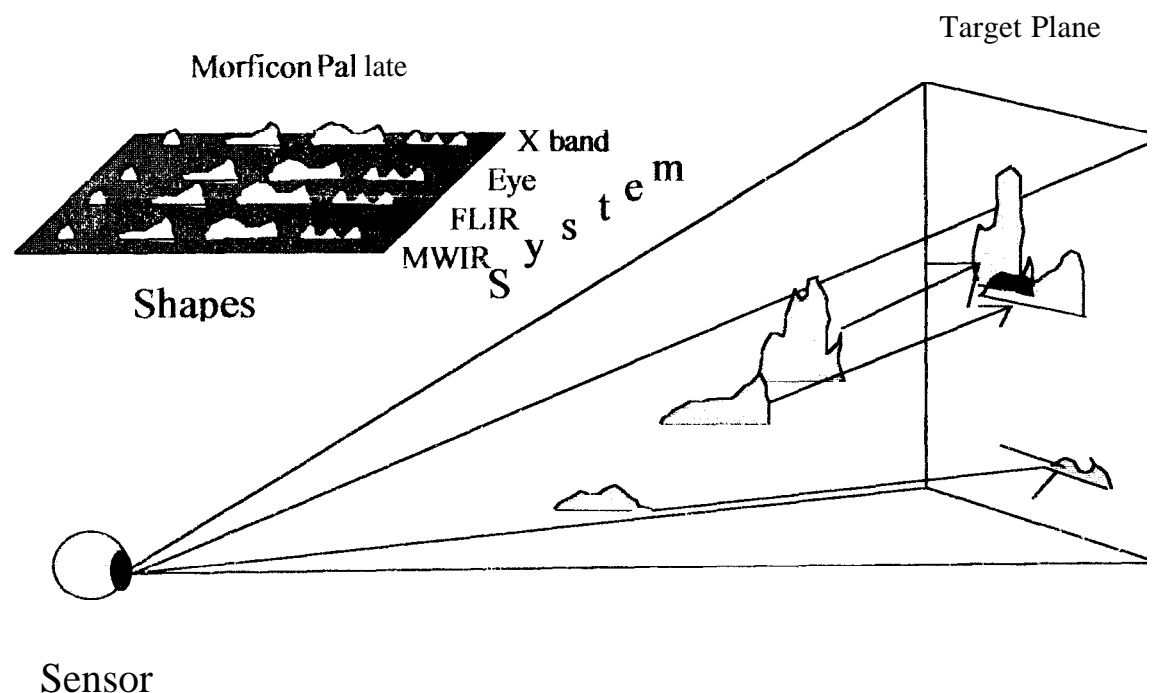


FIGURE 2 The transmission of various object is rapidly projected onto a plane at the distance of the target. Values on this plane can be added to objects beyond the target plane to produce a background plane.

With a morficon, the exact value of the distance through an object (e.g. a cloud) is known. Also the exact value of transmission or other parameter is know. These values are summed up by adding morficons to a target plane. The results are exact line-of-sight integrations – to within computer precision. See Figure 2.

A pallet of **morficons** is used to provide calculations for various sensors and atmospheric structures. **Usually** there is a tradeoff between speed and accuracy. With the **morficon**, both ultra-speed and accuracy result. Part of this advantageous situation is due to the **prior** calculation in making the **morficon** palette.

4.2 STOCHASTIC INDEXING

Rather than store **all** the information for viewing from different angles, the reproducibility property of pseudo-random number generators is used to index location and properties **of** each object. This “Stochastic Indexing” **allows** for millions of objects to be specified and retrieved with nearly zero storage. A backward running random number generator **allows** desired properties (e.g. 95% coldest temperature) to be generated. Algorithms are described and computer routines are presented in Boehm and **Willand** (1996). An illustrative demonstration of stochastic indexing is found in Boehm (1994b).

The typical computer random number generator starts with a seed number and rapidly returns one or more numbers -- a sequence -- that appears to be random. However, if the same starting seed is used, the exact same sequence will result.

Many types of scene-generating algorithms use this feature to produce the same **scene** by using the same seed. But if only a part of the scene is needed, the whole scene must be redone in order to obtain that section of the sequence pertinent to the desired part. If an inverse Fourier transform method is used, the whole random sequence must be calculated to get the random phases (the amplitudes are usually set to produce a desired spatial spectrum).

Stochastic Indexing goes one step **further**. it uses multiple starting seeds to generate what is needed at a point. The advantage of stochastic indexing is that the **very** large number of objects required for intricate detail can be indexed rapidly without a huge data base.

4.3 HEFeS (Hierarchical Environmental Feature Structure)

A hierarchy of feature objects, see Table 1, has been devised to **specify** structure over the scales of interest. We know from work reported in **Boehm** et al. (1993) and **Eis** (1997) that structure is not. scale invariant. That is, structures at one **scale** do not **occur** at the same frequency (**or** sometimes at all) at other scales. To say the same thing another way, some of the terms in the equations of motion that are dominant at one **scale** are negligible at other scales.

The location and orientation of sub-objects are relative to the parent object. This technique allows rapid sorting of objects as **to** whether they are in a view or not, since the sub-objects do not need to be checked if the parent object is out of view.

TABLE 1 Typical HEFeS Objects

OBJECT CLASS	TYPICAL SIZE	TYPICAL TIME	EXAMPLE
Climate regime	global	1 month	wet spring
planetary wave	5000km	1 week	zonal jet
synoptic feature	1000km	3 days	cold front
meso feature	100km	12 hours	squall line
cluster	1km	1 hour	cloud cluster
cell	30m	10 min.	cloud cell
sheet	5m	5 min	rain streamer
voxel	1m	10 sec.	droplet dist.
particle	1mm	1 sec	snow flake

4.4 Climatology to Simulation Parameters – PARGET

The purpose of PARGET, ‘Parameter GETer’, is to **specify** the parameters of the simulated atmosphere so that it is representative of a given location, season, time of day and/or desired weather. PARGET transforms general user specifications into parameters required to establish a specific HEFeS Specification. PARGET consists of five sections: 1. Input Interface, 2. Output Interface, 3. Logic Section, 4. Stochastic **selection**, and 5. HEFeS Climate Data. Only a portion of PARGET will be discussed here, namely the types of input and an illustrative example of stochastic selection from a climatic distribution.

4.4.1 The input to PARGET is **location**, time of day, time of **year**, and kind of selection. The kind of selection is **one** of three:

4.4.1.1 A random draw from **the** appropriate **climate**.

4.4.1.2 A selection of a percentage and a condition for the percent worst observed condition. The condition may be a single variable, rain **rate**, or it may be a joint condition such as the lowest ceiling and/or visibility.

4.4.1.3 A specified feature. The feature **may** be a desired condition such **as** a large thunderstorm right there. The feature may also be a point observation or forecast, - e.g. a METAR surface observation or TAF. The specified feature may be at any scale. For example, the feature may also **be** a synoptic field. (See **Boehm**, 1995) or it could be a droplet on a sensor’s **lens**. In either case, the other **scales** of objects are selected to be consistent with the specified feature.

4.4.2 An illustrative **example** of stochastic selection is the rain rate for Northern Israel. Based on the algorithms developed by **Tattleman** et al. (1995), it was found that the climatic probability of **rain** rate for the month of February is,

$$p = \Phi [3.5 + 0.955 \text{ Ln } (R)] \quad (3)$$

where P is the probability, R is the rain rate in mm/min, and Φ is the cumulative normal function.

Equation 3 is easily inverted to find the rain rate that corresponds to a specified probability,

$$R = \exp[\Phi^{-1}(P) - 3.5 / 0.955] \quad (4)$$

where Φ^{-1} is the inverse cumulative normal distribution.

Thus, if the percent heaviest, P, is specified, the corresponding rain rate, R, for northern Israel in February can be calculated for use in simulating the 100 P percent heaviest precipitation. Following Tattleman (1994) the Liquid Water Content, LWC, can also be calculated,

$$\text{LWC} = 0.052 R^{0.864} \quad (5)$$

5. Recapitulation

The HEFeS/Stochastic Indexing/Morfiction combination is an accurate, very fast method for simulation of weather impacts in a relatively small inexpensive program. Some desirable capabilities such as the 95% worst simulation are hard to do any other way.

Many people have trouble grasping the stochastic generator concepts. They appear too simple. However, the underlying laws are quite complex indeed. To some they appear as Voodoo. However, stochastic laws rest on theorems and proofs much tighter than most meteorological derivations.

6. ACKNOWLEDGMENTS

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